

Semantics

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Logical languages

Semantic parsing

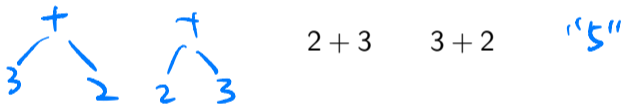
Syntax vs semantics

Syntax: does the string belong to the language?

Semantics: what is the meaning of the string?

Examples in programming languages:

Different syntax, same semantics



Same syntax, different semantics

3 / 2 (Python 2.7) 3 / 2 (Python 3)
1 1.5

(Slide adapted from Stanford CS221 Lecture 16)

Model-theoretic semantics

An **expression** is a string of mere symbols.

A **model** defines meanings of symbols.

The output of an expression with respect to a model is its **denotation**.

expression	model	denotation
<code>3 + 2 * 4</code>	calculator	11
<code>the red ball</code>	an image	the red ball in the image
<code>SELECT Name FROM Student WHERE Id = 0;</code>	database	John
<code>Book me a ticket from NYC to Seattle</code>	database	[action]

We understand the expression if we know how to act (in a world).



Natural language as expressions

Motivating applications:

Question answering

What is the profit of Mulan?

Who is the 46th president of the US?

Personal assistant

Alexa, play my favorite song.

Siri, show me how to get home.

- ▶ But natural language is full of ambiguities
- ▶ Cannot be directly handled by a computer (unlike programming/formal languages)

Semantic analysis

Goal: convert natural language to meaning representation

John likes fruits. (*informal*)

$\forall x \text{ FRUIT}(x) \implies \text{LIKES}(x, \text{JOHN})$ (*formal*)

Main tool: first-order logic

Why logic?

- ▶ Unambiguity: one meaning per statement
- ▶ Knowledge: link symbols to knowledge (entities, relations, facts etc.) (*Take in complex information*)
- ▶ Inference: derive additional knowledge given statements (*Reason with the information*)

Logic and semantics: example

Natural language: “John likes Mary’s friends”

Logical form: $\forall x \text{ FRIENDS}(x, \text{MARY}) \implies \text{LIKES}(x, \text{JOHN})$

World model: state of affairs in the world

People = {John, Mary, Joe, Ted}

John is a friend of Mary.

Joe is a friend of Mary.

Given the world model,

- ▶ Is $\text{LIKES}(\text{JOE}, \text{JOHN})$ true?
- ▶ What else can we infer from the statement?

The value of the expression may change given a different world model.

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Propositional logic

A **proposition** is a statement that is either true or false.

Propositional logic deals with propositions and their relations.

Syntax of propositional language:

- ▶ **Propositional symbols:** a *primitive* set of propositions

p_1 : John likes Mary

p_2 : John is a student

- ▶ **Logical connectives:** rules to build up **formulas**

symbol	read	meaning	formula
\neg	not	negation	$\neg p$
\vee	or	disjunction	$p \vee q$
\wedge	and	conjunction	$p \wedge q$
\implies	implies / if then	implication	$p \implies q$
\iff	equivalent to / iff	equivalence	$p \iff q$

- ▶ Parentheses: (,)



Parsing a formula

How would you check if a formula is valid (i.e. grammatical)?

A propositional formula is constructed by connecting propositions using the connectives.

- ▶ Formulas can be nested.
- ▶ Parentheses are used to disambiguate formulas.

Example:

$$((p \wedge q) \wedge \neg p)$$

$$((p \vee q) \wedge r) \implies p$$

Try to draw the parse trees of the formulas.

World model for propositional logic

Propositional symbols:

$p_1 = \text{hot}$

$p_2 = \text{John likes ice cream}$

$p_3 = \text{John ate an ice cream}$

Formula: $p_1 \wedge p_2 \implies p_3$ (Is this true?)

World model for propositional logic

Propositional symbols:

$p_1 = \text{hot}$

$p_2 = \text{John likes ice cream}$

$p_3 = \text{John ate an ice cream}$

Formula: $p_1 \wedge p_2 \implies p_3$ (Is this true?)

The **world model** in propositional logic is an *assignment* of truth values to propositional symbols.

	m_1	m_2	m_3	m_4	m_5	m_6	m_7	m_8
p_1	T	T	T	T	F	F	F	F
p_2	T	T	F	F	T	T	F	F
p_3	T	F	T	F	T	F	T	F

In which world(s) is the above formula false?

Meaning of a formula

Propositional symbols:

$p_1 = \text{hot}$

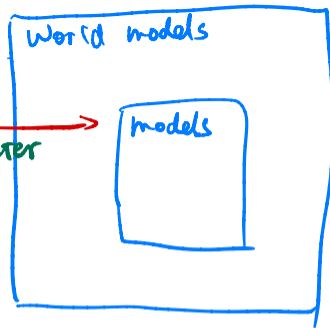
$p_2 = \text{John likes ice cream}$

$p_3 = \text{John ate an ice cream}$

Formula: $p_1 \wedge p_2 \implies p_3$ *Just symbols!*

formula
symbols

interpreter



Semantics is given by *interpreting* the formula against a world model.

A formula specifies *a set of world models* where it is true.

A set of formulas is a knowledge base (constraints on the world model).

Making inference given formulas and the world model: take a course in AI.

Limitations of propositional logic

How do we represent knowledge of a *collection* of objects?

“Everyone who likes ice cream ate an ice cream.”

p_{JOHN} (John likes ice cream) \implies q_{JOHN} (John ate an ice cream)

p_{JOE} (Joe likes ice cream) \implies q_{JOE} (Joe ate an ice cream)

p_{ALICE} (Alice likes ice cream) \implies q_{ALICE} (Alice ate an ice cream)

p_{CAROL} (Carol likes ice cream) \implies q_{CAROL} (Carol ate an ice cream)

...

[] likes ice cream \implies [] ate an ice cream

Need a compact way to represent a collection of objects!

First-order logic

First-order logic generalizes propositional logic with several new symbols:

Represent objects:

Constants Primitive objects, e.g. John

Variables Placeholder for some object, e.g. x

Functions A map from object(s) to an object, e.g. John \rightarrow John's farther

Group objects:

Predicate Properties of a set of objects, e.g. students, couples

Quantify a (infinite) set of objects:

Quantifiers Specify the number of objects with a certain property, e.g. *all* people are mortal.

Constants, variables, functions

Constants refer to primitive objects such as named entities:

JOHN, ICECREAM, HOT

A **variable** refers to an unspecified object:

x, y, z

STUDENT(x)

FRIENDS(x , JOHN)

A n -ary **function** maps n objects to an object:

MOTHER(x)

FRIENDS(MOTHER(x), MOTHER(y))

Predicates

A **predicate** is an indicator function $P: X \rightarrow \{\text{true}, \text{false}\}$.

- ▶ Describes properties of object(s)

- ▶ $P(x)$ is an atomic formula

STUDENT(MARY)

SMALLER(DESK, COMPUTER)

FRIENDS(JOHN, MARY) \implies FRIENDS(MARY, JOHN)

Quantifiers

Universal quantifier \forall :

- ▶ The statement is true for *every* object
- ▶ $\forall x P(x)$ is equivalent to $P(A) \wedge P(B) \wedge \dots$
- ▶ All people are mortal: $\forall x \text{PERSON}(x) \implies \text{MORTAL}(x)$

Existential quantifier \exists :

- ▶ The statement is true for *some* object
- ▶ $\exists x P(x)$ is equivalent to $P(A) \vee P(B) \vee \dots$
- ▶ Some people are mortal: $\exists x \text{PERSON}(x) \wedge \text{MORTAL}(x)$

Order matters, e.g., “everyone speaks a language”:

$$\forall x \exists y \text{SPEAKS}(x, y)$$

$$\exists y \forall x \text{SPEAKS}(x, y)$$

Syntax of first-order logic

Terms refer to objects:

- ▶ Constant symbol, e.g. JOHN
- ▶ Variable symbol, e.g. x
- ▶ Function of terms, e.g. MOTHER(x), CAPITAL(NY)

Formula evaluates to true or false:

- ▶ Predicate over terms is an atomic formula, e.g. STUDENT(MOTHER(JOHN))
- ▶ Connectives applied to formulas (similar to propositional logic)

$$\text{STUDENT}(x) \wedge \text{HAPPY}(x)$$

- ▶ Quantifiers applied to formulas

$$\forall x \text{ STUDENT}(x) \implies \text{HAPPY}(x)$$

$$\exists x \text{ STUDENT}(x) \wedge \text{HAPPY}(x)$$

World model of first-order logic

How do we know if FRIENDS(JOHN, MARY) is true?

World model of propositional logic: **propositions**

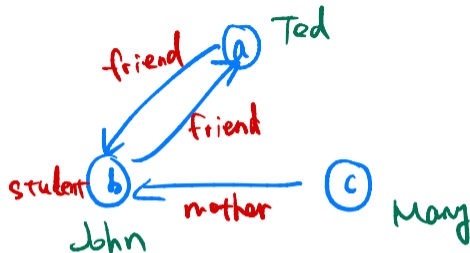
proposition	truthful value
John is a friend of Mary	True
John is a friend of Joe	False

World model of first-order logic: **objects and their relations**

constant symbol	object
JOHN	a
MARY	b

predicate symbol	set of n -tuples
FRIENDS	$\{(a, b), (b, a)\}$

Graph representation of the world model



const symbols

$$\text{friend} = \{(a, b), (b, a)\}$$

$$\text{mother} = \{(c, b)\}$$

$$\text{student} = \{a, b\}$$

$$\text{families} = \{(a, b, c), \dots\}$$

Summary

Syntax produces symbols and well-formed formulas.

Semantics grounds symbols to a world and allows for evaluation of formulas.

We have seen how it works for formal languages such as propositional logic and first-order logic.

Next, formal language to natural language.

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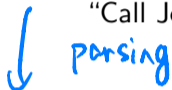
Logical languages

Semantic parsing

System overview

Utterance Linguistic expression.

"Call John, please."



Logical form Formal meaning representation of the utterance

CALL(JOHN) *program*



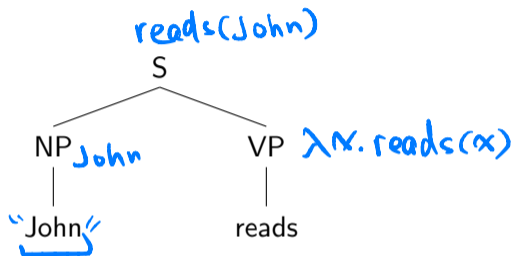
Denotation Output of the meaning representation with respect to the model

Calling XXX-XXX-XXXX ... *execution result*



Translate NL to logical language

Key idea: *compositionality*



- ▶ Sentence: READS(JOHN) (What's the denotation?)
- ▶ We would like to construct it recursively
 - ▶ John: JOHN (a unique entity)
 - ▶ reads: a predicate (function) that takes an entity (one argument)

A brief introduction to lambda calculus

Lambda calculus / λ -calculus

- ▶ A notation for applying a function to an argument

$$\lambda x. x^2 + x$$

$f: x \mapsto x^2 + x$

- ▶ A function that is waiting for the value of a variable to be filled
- ▶ Function application by β -reduction

$$(\lambda x. x^2 + x)(2) = 2^2 + 2 = 6$$

- ▶ Takes multiple arguments by “currying”

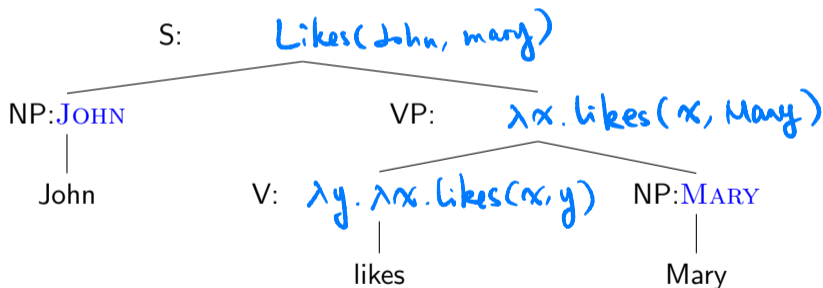
$$(\lambda x. \lambda y. xy)(2) = \lambda y. 2y$$

$$(\lambda x. \lambda y. xy)(3)(2) = (\lambda y. 2y)(3) = 6$$

Translate NL to logical language

Verbs are predicates

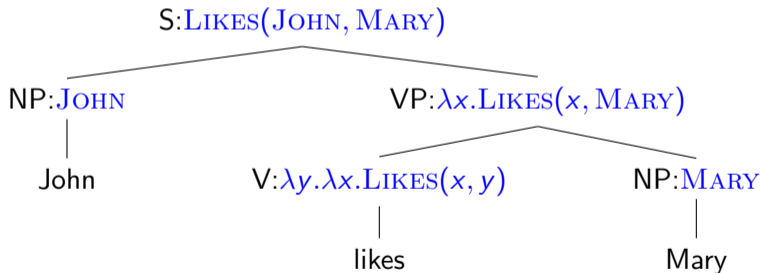
- ▶ reads: $\lambda x. \text{READS}(x)$ (waiting for an NP)
- ▶ likes: $\lambda x. \lambda y. \text{LIKES}(x, y)$ (waiting for two NPs)



Translate NL to logical language

Verbs are predicates

- ▶ reads: $\lambda x. \text{READS}(x)$ (waiting for an NP)
- ▶ likes: $\lambda x. \lambda y. \text{LIKES}(x, y)$ (waiting for two NPs)



Compositional semantics

Bottom up parsing:

- ▶ Start with the semantics of each word
- ▶ Combine semantics of spans according to certain rules
 - ▶ Associate a combination rule with each grammar rule

$V:\lambda y.\lambda x.LIKES(x, y)$	\rightarrow	likes
$NP:JOHN$	\rightarrow	John
$VP:\alpha(\beta)$	\rightarrow	$V:\alpha$ $NP:\beta$
$S:\beta(\alpha)$	\rightarrow	$NP:\alpha$ $VP:\beta$

- ▶ Get semantics by function application
- ▶ Lexical rules can be complex!

Quantification

John bought a book

BOUGHT(JOHN, BOOK)?

“book” is not a unique entity! BOUGHT(MARY, BOOK)

Correct logical form: $\exists x \text{BOOK}(x) \wedge \text{BOUGHT}(\text{JOHN}, x)$

But what should be the semantics of “a”? $\lambda P. \lambda Q. \exists x P(x) \wedge Q(x)$

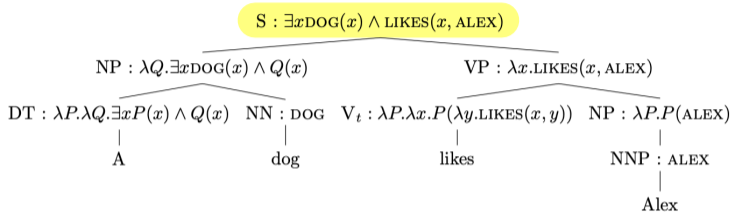
“a book”: $\lambda Q. \exists x \text{BOOK}(x) \wedge Q(x)$. (Need to change other NP rules)

What about “the”, “every”, “most”?

We also want to represent tense: “bought” vs “will buy”. (event variables)

Learning from derivations

Text: John bought a book (utterance)



Annotation:

Use approaches from (discriminative) constituent parsing

Obstacles:

- ▶ Derivations are rarely annotated.
- ▶ Unlike syntactic parsing, cannot obtain derivations from logical forms.
- ▶ Spurious derivation: wrong derivations that reach the correct logical form.

Learning from logical forms

Text: John bought a book (utterance)

Annotation: $\exists x \text{BOOK}(x) \wedge \text{BOUGHT}(\text{JOHN}, x)$ (logical form)

Key idea: model derivation as a latent variable z [Zettlemoyer and Collins, 2005]

Learning: maximum marginal likelihood

$$\begin{aligned} \log p(y | x) &= \log \sum_z p(y, z | x) \\ &= \log \sum_z \frac{\exp(\theta \cdot \Phi(x, y, z))}{\sum_{z', y'} \exp(\theta \cdot \Phi(x, y', z'))} \end{aligned}$$

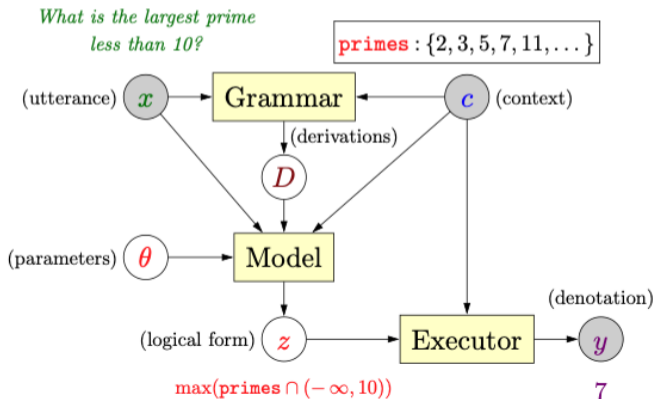
- ▶ Need to learn both the lexicon and the model parameters (for CCG)
- ▶ Use EM algorithm (with approximation)

Learning from denotations

Text: What states border Georgia?

Annotation: Alabama, Florida, North Carolina, South Carolina, Tennessee

Key idea: model the logical form as a latent variable z [Liang, 2013]



Datasets

Geo880

- ▶ 880 questions and database queries about US geography
- ▶ “what is the highest point in the largest state?”
- ▶ Compositional utterances in a clean, narrow domain

ATIS

- ▶ 5418 utterances of airline queries and paired logical forms
- ▶ “show me information on american airlines from fort worth texas to philadelphia”
- ▶ More flexible word order but simpler logic

Free917, WebQuestions

- ▶ Questions and paired logical forms on Freebase
- ▶ Logically less complex but scales to many more predicates

Text to SQL

Spider (Yu et al. 2018)

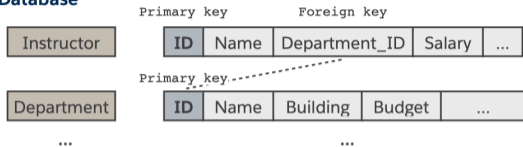
Expert-annotated, cross-domain, complex text-to-SQL dataset

Assumption:

- For each

	Train	Dev	Hidden
# DBs	146	20	40
# Examples	8,659	1,034	2,147

Database



Question What are the name and budget of the departments with average instructor salary above the overall average?

SQL

```
SELECT T2.name, T2.budget
FROM Instructor AS T1 JOIN Department AS T2 ON
T1.Department_ID = T2.ID
GROUP BY T1.Department_ID
HAVING AVG(T1.salary) >
(SELECT AVG(Salary) FROM Instructor)
```

(Slide from Victoria Lin)

Challenges

Design the logical representation and grammar

- ▶ Expressivity vs computation efficiency
- ▶ Domain-specific vs domain-general
- ▶ Interacts with annotation and learning

Learning from different supervision signals

- ▶ End-to-end (utterance to action)
- ▶ Reinforcement learning (robotics, visual grounding)
- ▶ Interactive learning (obtain user feedback)