Context-Free Parsing

He He

New York University

October 27, 2020

2

1

5900

Logistics

- Homework 3
- Project proposal and group
- Project presentation

3

5900

<ロト < 同ト < 三ト < 三ト

Table of Contents

1. Context-free language

2. Probabilistic context-free grammars

3. Discriminative parsing

<ロト < 同ト < 三ト < 三ト

æ

Langauge is a set of strings

Formal language:

- A set of strings consisting of words from an alphabet
- Well-formed according to a set of rules
- Studies the syntactical aspects of a language

Examples:

- Formulas (logic): $(p_1 \land p_2) \lor (\neg p_3)$ ($\bigcirc P_1$
- Programming languages: int a, b = 0;
- Sequences from the alphabet {a, b} that ends with two a's

Questions:

- Formal language theory: expressiveness power, recognizability etc.
- Can we design formal languages that capture as many properties of natural language as possible?

SQ (V

Context-free language

Context-free languages (CFL) are generated by a **context-free** grammar $G = (\Sigma, N, R, S)$:

- a finite alphabet Σ of terminals (words)
- a finite set of non-terminals N disjoint from Σ (word groups)
- ► a set of **production rules** *R* of the form $A \rightarrow \beta$, where $A \in N, \beta \in (\Sigma \cup N)^*$ (how to group words)
- ▶ a start symbol $S \in N$ (root of derivation)

Example:

$$S \rightarrow SS$$

 $S \rightarrow (S)$
 $S \rightarrow ()$

3

SQ Q

-∢∃>

< D > < A < > < < >

Natural language syntax

Construct a formal language to represent the syntax of natural language

- Expressivity: how many syntactic phenomena can it cover?
- Computation: how fast can we parse a sentence?

Context-free grammars for natural language

- Captures nested structures which are common in natural language [I told Mary that [John told Jane that [Ted told Tom a secret]]].
- Captures long-range dependencies

the burnt and badly-ground Italian coffee these burnt and badly-ground Italian coffees

Strikes a good balance between expressivity and computation

SQ Q

Phrase-structure grammar for English

Sentences are broken down into **constituents**.

A constituent works as a single unit in a sentence.

Can be moved around or replaced without breaking grammaticality. (Abigail) and (her younger brother) (bought a fish).

Construct CFG for English

- Each word is a terminal, derived from its POS tag.
- Each sentence is derived from the start symbol *S*.
- Each phrase type is a non-terminal.
- Each constituent is derived from a non-terminal.

Grammar design: choose the right set of non-terminals that produces different constituents.

3

SQ Q

A toy example CFG

R =

$$N = \{S, NP, VP, PP, DT, Vi, Vt, NN, IN\}$$

$$S = S$$

 $\Sigma = \{$ sleeps, saw, man, woman, dog, telescope, the, with, in $\}$

S	\rightarrow	NP	VP
VP	\rightarrow	Vi	
VP	\rightarrow	Vt	NP
VP	\rightarrow	VP	PP
NP	\rightarrow	DT	NN
NP	\rightarrow	NP	PP
PP	\rightarrow	IN	NP

Vi	\rightarrow	sleeps
Vt	\rightarrow	saw
NN	\rightarrow	man
NN	\rightarrow	woman
NN	\rightarrow	telescope
NN	\rightarrow	dog
DT	\rightarrow	the
IN	\rightarrow	with
IN	\rightarrow	in

Lexicon: rules that produce the terminals

(日)

October 27, 2020 8 / 32

3

SQ (2)

Darcing		זררז	
Parsing	uplosthe	lunnan jy	[v: sleeps]]]

R =

S	\rightarrow	NP	VP
VP	\rightarrow	Vi	
VP	\rightarrow	Vt	NP
VP	\rightarrow	VP	PP
NP	\rightarrow	DT	NN
NP	\rightarrow	NP	PP
PP	\rightarrow	IN	NP

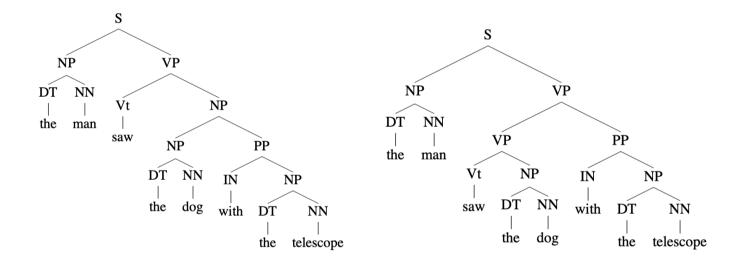
\rightarrow	sleeps
\rightarrow	saw
\rightarrow	man
\rightarrow	woman
\rightarrow	telescope
\rightarrow	dog
\rightarrow	the
\rightarrow	with
\rightarrow	in
	$\begin{array}{c c} \uparrow \\ \uparrow $

Can we derive the sentence "the man sleeps"?

S
$$\rightarrow$$
 NP VP
 \rightarrow DT NN VP
 \rightarrow the NN VP
 \rightarrow the man VP
 \rightarrow the man Vi
 \rightarrow the man stars
He He (NYU) CSCI-GA.2590 October 27, 2020 9/32

Ambiguity

Can a sentence have multiple parse trees?



Exercise: find parse trees for "She announced a program to promote safety in trucks and vans".

CSCI-GA.2590

Э

SQ (2)

э.

< f

< □ ▶

Table of Contents

1. Context-free language

2. Probabilistic context-free grammars

3. Discriminative parsing

<ロト < 同ト < 三ト < 三ト

3

Notation: let \mathcal{T}_G be the set of all possible left-most parse trees under the grammar G.

Goal: define a probability distribution p(t) over parse trees $t \in \mathcal{T}_G$

Parsing: pick the most likely parse tree for a sentence s

 $\arg \max p(t)$ $_{t \in \mathcal{T}_G(s)}$

Three questions:

- Modeling: how to define p(t) for trees?
- Learning: how to estimate parameters of the distribution p(t)?
- Inference: how to find the most likely tree efficiently?

◆□▶ ◆□▶ ▲三▶ ▲三▶ 三 ���

Modeling

Generate parse trees: iteratively sample a production rule to expand a non-terminal

R =				
	S	\rightarrow	NP	VP
	VP	\rightarrow	Vi	
	VP	\rightarrow	Vt	NP
	VP	\rightarrow	VP	PP
	NP	\rightarrow	DT	NN
	NP	\rightarrow	NP	PP
S	PP	\rightarrow	IN	NP
NP VP) PP			

Vi	\rightarrow	sleeps
Vt	\rightarrow	saw
NN	\rightarrow	man
NN	\rightarrow	woman
NN	\rightarrow	telescope
NN	\rightarrow	dog
DT	\rightarrow	the
IN	\rightarrow	with
IN	\rightarrow	in

< □ ▶

< 47 ▶

< ∃ >

э.

3

PCFG

A PCFG consists of

• A CFG $G = (\Sigma, N, R, S)$

▶ Probabilities of production rules $q(\alpha \rightarrow \beta)$ for each $\alpha \rightarrow \beta \in R$ such that

$$\sum_{eta: X o eta \in R} q(X o eta) = 1 \quad orall X \in N$$

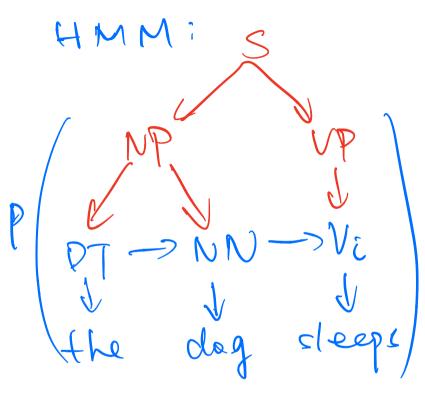
S	\rightarrow	NP	VP	1.0
VP	\rightarrow	Vi		0.3
VP	\rightarrow	Vt	NP	0.5
VP	\rightarrow	VP	PP	0.2
NP	\rightarrow	DT	NN	0.8
NP	\rightarrow	NP	PP	0.2
PP	\rightarrow	IN	NP	1.0

Vi	\rightarrow	sleeps	1.0
Vt	\rightarrow	saw	1.0
NN	\rightarrow	man	0.1
NN	\rightarrow	woman	0.1
NN	\rightarrow	telescope	0.3
NN	\rightarrow	dog	0.5
DT	\rightarrow	the	1.0
IN	\rightarrow	with	0.6
IN	\rightarrow	in	0.4

∃ ► < **∃** ►

3

From HMM to PCFG



p (the = P(DT, NN INP) P(V: |VP) P(VP, NPIS) P(S)

<ロト < 団 > < 国 > < 国 > < 国 >

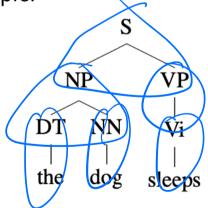
3

Probabilities of parse trees

Given a parse tree *t* consisting of rules $\alpha_1 \rightarrow \beta_1, \ldots, \alpha_n \rightarrow \beta_n$, its probabilities under the PCFG is

$$p(t) = \prod_{i=1}^{n} q(\alpha_i \to \beta_i) \bigvee_{V \not P} \bigvee_{V \not P}$$

Example:



<ロ > < 同 > < 三 > < 三 > < 三 > <

- **B**

Learning p(S->NPVP)

Given a set of trees, we can estimate rule probabilities by MLE.

SQ (~

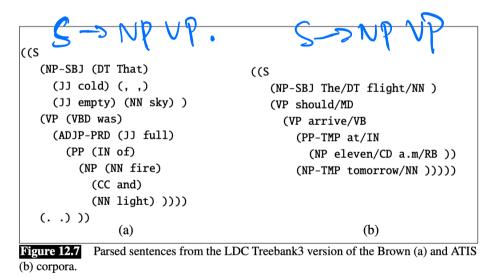
(日)

Learning

Given a set of trees, we can estimate rule probabilities by MLE.

$$q(\alpha \to \beta) = \frac{\operatorname{count}(\alpha \to \beta)}{\sum_{\beta' \colon \alpha \to \beta' \in R} \operatorname{count}(\alpha \to \beta')}$$

Training data: treebanks



CSCI-GA.2590

October 27, 2020 17 / 32

э.

 $\mathcal{A} \mathcal{A} \mathcal{A}$

<ロ > < 同 > < 同 > < 三 > < 三 >

Parsing

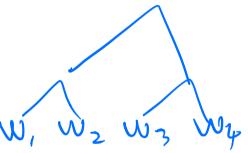
Input: sentences, (P)CFG

Output: derivations / parse trees (with scores/probabilities)

Total number of parse trees for a sentence?

Consider a minimal CFG:

 $X \rightarrow XX$ $X \rightarrow aardvark|abacus| \dots |zyther|$



of parse trees = # of strings with balanced brackets $((w_1w_2)(w_3w_4)), (((w_1w_2)w_3)w_4), ...$

of strings with n pairs of brackets:

Catalan number
$$C_n = \frac{1}{n+1} \binom{2n}{n}$$

▲ □ ▶ ▲ 三 ▶ ▲ 三 ▶

- B

SQ Q

Chomsky normal form (CNF)

A CFG is in **Chomsky normal form** if every production rule takes one of the following forms:

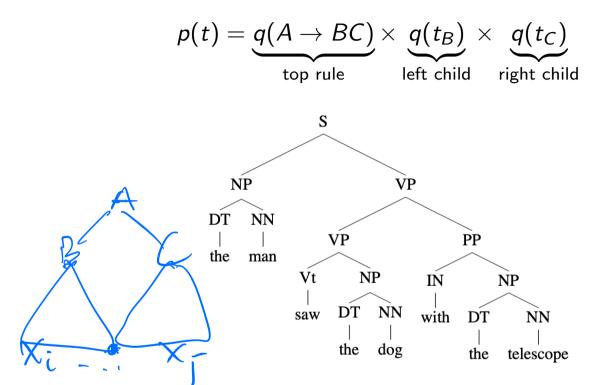
- Binary non-terminal production: $A \rightarrow BC$ where $A, B, C \in N$.
- Unary terminal production: $A \rightarrow a$ where $A \in N, a \in \Sigma$.

Grammars in CNF produces binary parse trees. Convert a production rule to CNF: $VP \rightarrow VBD$, $NP PP_1$ $VP \rightarrow VBD @VP-VBD$

SQ Q

< □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ >

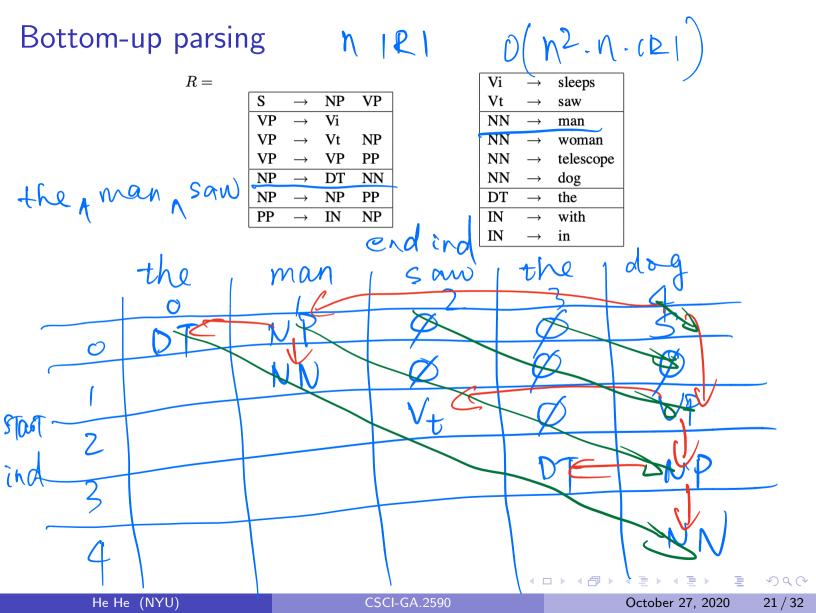
Dynamic programming on the tree



What are the variables when constructing a tree rooted at A spanning x_i, \ldots, x_j ?

- The production rule $A \rightarrow BC$
- ▶ The splitting point *s*: *B* spans x_i, \ldots, x_s and *C* spans x_{s+1}, \ldots, x_j

He He (NYU)



The CYK algorithm

Notation: $\mathcal{T}(i, j, X)$ is the set of trees with root node X spanning x_i, \ldots, x_j Subproblem:

$$\pi(i,j,X) = \max_{t \in \mathcal{T}(i,j,X)} p(t)$$

Base case:

$$\pi(i, i, X) = \begin{cases} q(X \rightarrow x_i) & \text{if } X \rightarrow x_i \in R \\ 0 & \text{otherwise} \end{cases}$$

Recursion:

$$\pi(i,j,X) = \max_{\substack{Y,Z \in N \\ s \in \{i,\dots,j-1\}}} q(X \to YZ) \times \pi(i,s,Y) \times \pi(s+1,j)$$

Use backtracking to find the argmax tree.

He He (NYU)

SQ (~

Variants of CYK

Argmax: find the most likely tree (analogous to Viterbi).

$$\pi(i,j,X) = \max_{s \in \{i,\dots,j-1\}} q(X \to YZ) \times \pi(i,s,Y) \times \pi(s+1,j)$$

Recognition: does the string belong to the language?

$$\pi(i,j,X) = \bigvee_{\substack{Y,Z \in N \\ s \in \{i,\dots,j-1\}}} \mathbb{I}[X \to YZ \in R] \wedge \pi(i,s,Y) \wedge \pi(s+1,j) \bigvee$$

Marginalization: what's the probability of the string being generated from the grammar? (the **inside algorithm**)

$$\pi(i,j,X) = \sum_{s \in \{i,\dots,j-1\}} q(X \to YZ) \times \pi(i,s,Y) \times \pi(s+1,j)$$

Complexity?

He He (NYU)

October 27, 2020 23 / 32

◆□▶ ◆□▶ ▲三▶ ▲三▶ 三 ���

Summary

	NB	НММ	PCFG
output structure	lategory	sequend	thee
learning		MLE	
decoding	prive for a	viterbî	CRY
marginalization		P(g; (x) P(g; - g; 1x)	$P(\hat{c}, \hat{j}, N \mid \mathcal{A})$
unsupervised learning		EM	

CSCI-GA.2590

590

< □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ >

Table of Contents

1. Context-free language

2. Probabilistic context-free grammars

3. Discriminative parsing

<ロ > < 同 > < 同 > < 三 > < 三 >

3

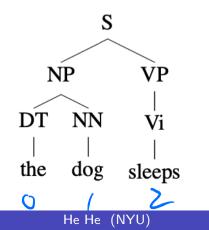
CRF for trees

Input: sequence of words $x = (x_1, ..., x_n)$ Output: parse tree $y \in \mathcal{T}(x)$ Model: decompose by production rules

$$p(y \mid x; \theta) \propto \prod_{(r,s)} \psi(r, s \mid x; \theta)$$

r: production rule

s: start, split, end indices of the rule r



$$\psi(S \rightarrow NP VP, (0, 1, 2))$$

 $\psi(NP \rightarrow DT ND, (0, 0, 1))$

SQ Q

CRF parsing

Potential functions:

$$\psi(r, s \mid x; \theta) = \exp\left(\theta \cdot \phi(r, s, x)\right)$$
$$\prod_{(r,s)\in\mathcal{T}(x)} \psi(r, s \mid x; \theta) = \exp\left(\sum_{(r,s)\in\mathcal{T}(x)} \theta \cdot \phi(r, s, x)\right) / \mathcal{Y}$$

Learning: MLE (P(y)x)

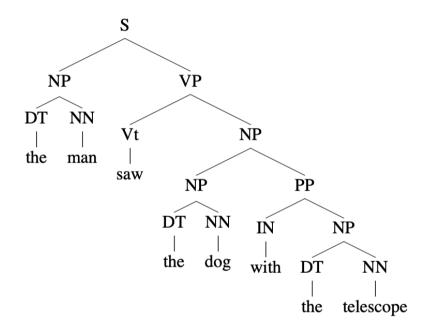
- 1. Compute the partition function by the inside algorithm
- 2. Call autograd to compute the gradient (backpropagation)

Inference: CYK

SQ Q

· < 同 > < 三 > < 三 > · 三

Limitations of PCFG



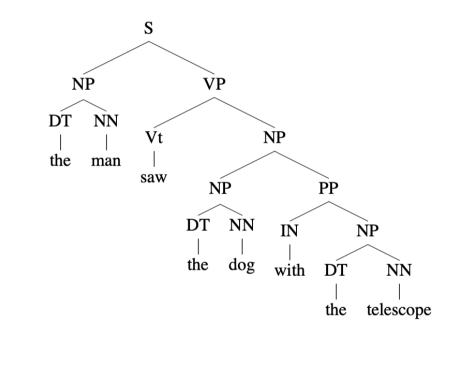
CSCI-GA.2590

1

590

<ロト < 団 > < 巨 > < 巨 >

Limitations of PCFG



Limit No lexical information

CSCI-GA.2590

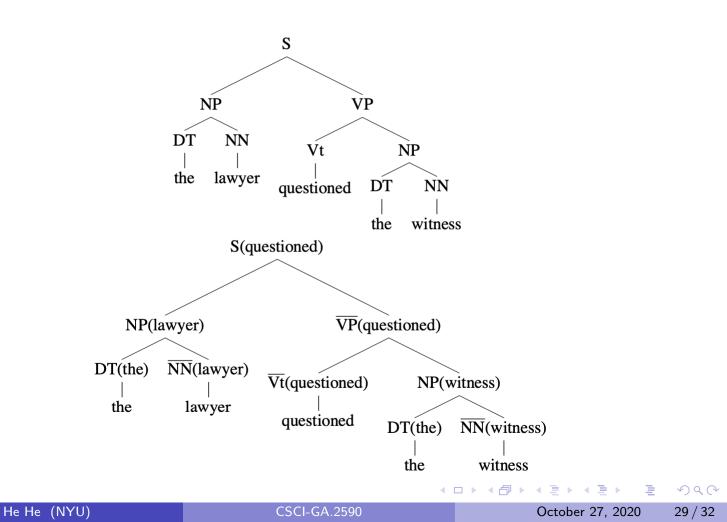
October 27, 2020 28 / 32

王

5900

Lexicalized PCFG

Attach the "head" of the span to each non-terminal



Features

local score = $\theta \cdot \phi(VP \rightarrow VBD NP, (5, 6, 8), \dots$ averted financial disaster...)

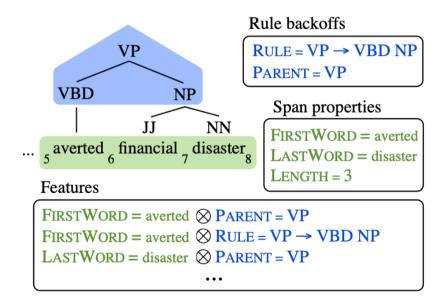


Figure: Less grammar, more features. [Hall+ 14]

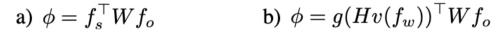
He He (NYU)

CSCI-GA.2590

October 27, 2020 30 / 32

◆□▶ ◆□▶ ◆三▶ ◆三▶ 三 のへぐ

Neural CRF parser



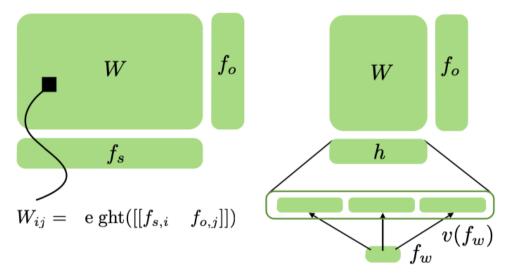


Figure: Neural CRF Parsing. [Durrett+ 15]

CSCI-GA.2590

3

5900

Evaluation



$$recall = \frac{\#correct \ constituents}{\#total \ constituents \ in \ gold \ trees}$$

 $precision = \frac{\#correct \ constituents}{\#total \ constituents \ in \ predicted \ trees}$

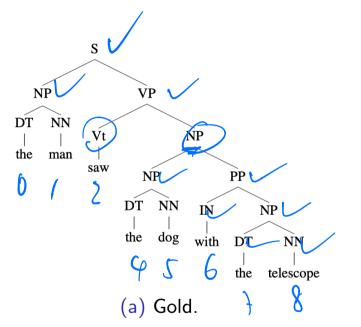
$$\mathsf{F1} = \frac{2 \times \mathsf{precision} \times \mathsf{recall}}{\mathsf{precision} + \mathsf{recall}}$$

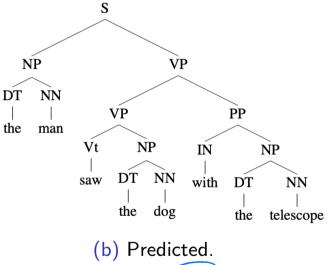
Labeled F1: the non-terminal node label must be correct

Unlabeled F1: just consider the tree structure

Example

(0,8,S) (0,1, MP) ...





CSCI-GA.2590

3