# Efficient Pretraining and Finetuning Techniques

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March 21, 2023

#### Logistics

- HW3 released: finetuning BERT!
- Proposal due today and we'll provide brief feedback on Gradescope (or come to OH)
- Midterm grades will be released soon.

## Introduction

Plan for today:

- How to train larger models on larger data with less compute
- How to finetune larger models with less compute

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- How to train larger models on larger data with less compute
- How to finetune larger models with less compute

Why care about efficiency?

- Practical reasons: training and running these models are expensive!
- Methods that help scaling may eventually leads to *better* models (e.g., transformers)

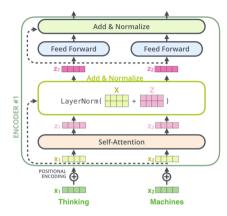
"The bitter lesson is based on the historical observations that 1) AI researchers have often tried to build knowledge into their agents, 2) this always helps in the short term, and is personally satisfying to the researcher, but 3) in the long run it plateaus and even inhibits further progress, and 4) breakthrough progress eventually arrives by an opposing approach based on scaling computation by search and learning." — Richard Sutton "The bitter lesson"

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**Efficient finetuning** 

#### **Transformer recap**



#### Which components require matrix multiplication?

#### Figure: From The Illustrated Transformer

#### **Transformer recap**

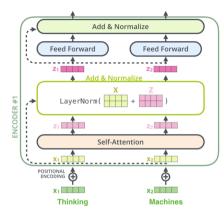


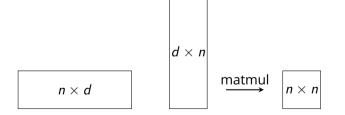
Figure: From The Illustrated Transformer Which components require matrix multiplication?

- Self-attention
  - Q,K,V projection
  - Scaled dot-product attention
- Feed-forward layer

Q, K, V projection:

$$n \times d_e$$
  $\xrightarrow{\text{linear}}$   $n \times d$ 

Scaled dot-product attention:

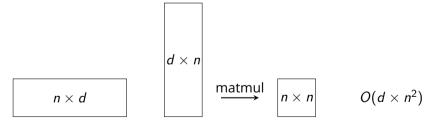


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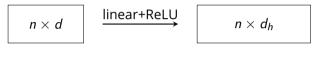
$$n \times d_e$$
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$$O(n \times d_e \times d)$$

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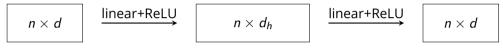


Feed-forward layer (GPT-2):



 $O(n \times d \times d_h)$ 

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 $O(n \times d \times d_h)$ 

- Two-layer FFN
- $d_h = 4d (d > 1K)$  by default in GPT-2
- Approximately half of the compute time

## Improve efficiency of transformers

How to scale transformer models to larger number of parameters and larger data?

- Quantization (training and inference)
- Weight sharing (training and inference)
- Sparsely-activated models (training and inference)
- Pruning (inference)
- Distillation (inference)

## Improve efficiency of transformers

This lecture: Improve efficiency of self-attention (for long sequences)

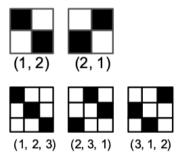
## Improve efficiency of transformers

This lecture: Improve efficiency of self-attention (for long sequences)

**Key idea**: reduce the  $O(n^2)$  time and memory cost

- Sparsify the attention matrix
  - Deterministic mask
  - Data-dependent mask
- Compress the key-value memory
  - Low-rank projection
  - Attention-based projection

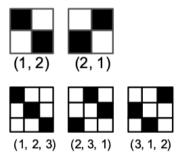
Blockwise self-attention [Qiu et al., 2020]: attention within a local window



#### **Masking Matrices**

- Divide a  $n \times n$  matrix into  $m \times m$  blocks
- Compute one block per row and mask the rest (i.e. set to 0)
- Allocate groups of attention heads to each mask configuration
  - Which configuration should use more attention heads?

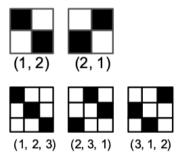
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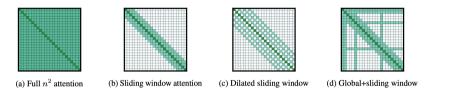
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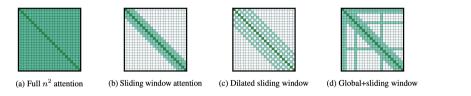
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- What's the time complexity?
  - $O(n^2) \longrightarrow O(n^2/m)$

Longformer [Beltagy et al., 2020]: attention within a local window



- Sliding window: attending to a *local* window of size w around each token  $O(n \times w)$
- Dilated sliding window: reaching *longer range* with a larger window size with gaps
- Global window: full attention on specific tokens, e.g., [CLS] in BERT

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- Global window: full attention on specific tokens, e.g., [CLS] in BERT
- Details: balancing efficiency and performance
  - Adding dilation on some heads
  - Using small window size on lower layers and larger ones on higher layers

**Reformer** [Kitaev et al., 2020]: attention within an adaptive local window **Key idea**:

$$a_i = \operatorname{softmax}\left(\left[rac{q_i \cdot k_1}{\sqrt{d}}, \dots, rac{q_i \cdot k_n}{\sqrt{d}}
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• We want to compute the attention scores for a query *q<sub>i</sub>*:

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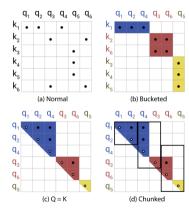
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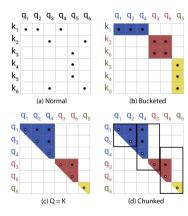
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- Compute attention between  $q_i$  and  $k_i$  only if they fall in the same hash bucket

Reformer [Kitaev et al., 2020] implementation



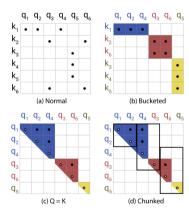
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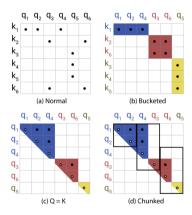
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(a) Leverage the sparsity of the attention matrixChallenge 1: find the nearest neighbors

(b) Sort *q*<sub>i</sub>'s and *k*<sub>i</sub>'s by their hash codes such that vectors in the same bucket are grouped

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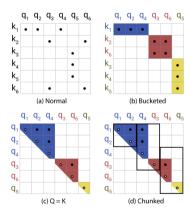


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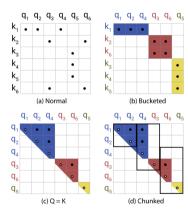
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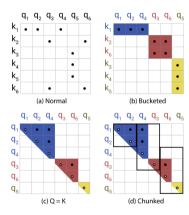
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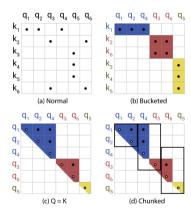
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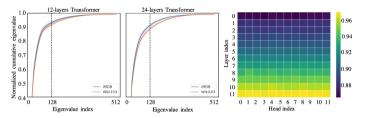


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Better accuracy with more hashes

# Summarize the KV memory

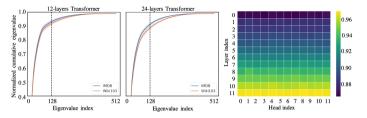
Self-attention is low rank [Wang et al., 2020]



• Left: cumulative eigenvalues of pretrained transformer with n = 512

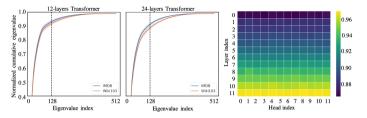
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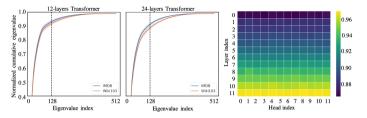
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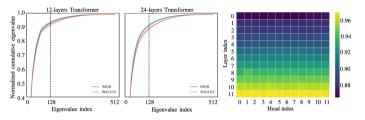
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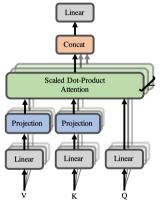
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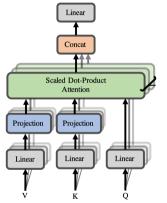
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- Idea: instead of attending to *n* tokens, attend to *k* principal components

**Linformer** [Wang et al., 2020]: compute self-attention in a lower dimension



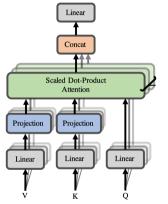
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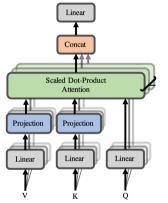


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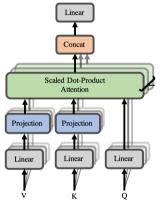
• Attend to the lower-dimensional memory: softmax  $\left(Q_{n \times d} \mathcal{K}_{k \times d}^{T} / \sqrt{d}\right)$ 



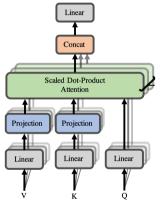
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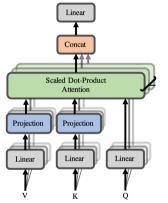
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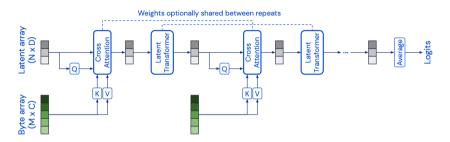


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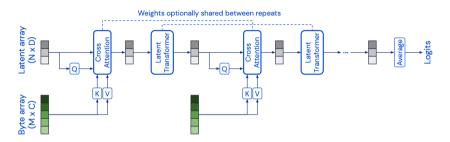
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  - Unclear how to mask: past and future are mixed

Perceiver [Jaegle et al., 2021]: use latent states to compress the KV memory



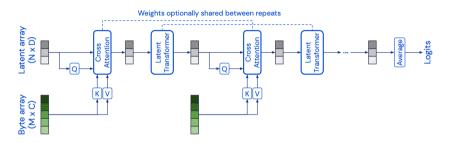
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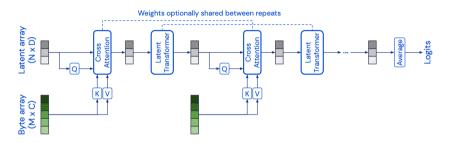
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- Map to latent states using cross attention: O(nm)
- Self-attention layers: O(Lm<sup>2</sup>)

Improve the quadratic time and space complexity of self-attention

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Bad news: Most techniques are not widely used in large pretrained models now. Why?

- Improvement in time/space complexity doesn't always translate to real time/space savings
- These techniques often breaks structure and sacrifice the batching ability on GPUs
- Only see improvement on very long sequences

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Takeaways:

- Attention structure is important
- Low-rank techniques

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Efficient finetuning

# Improve finetuning efficiency

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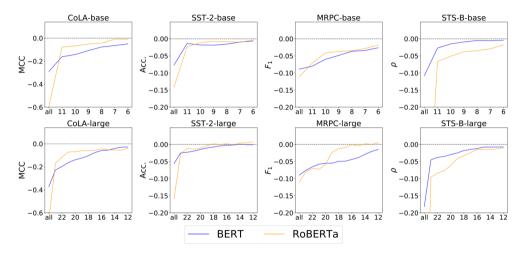
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- Saving and loading finetuned models for different tasks is costly.

Can we finetune a smaller number of parameters to achieve performance similar to full finetuning?

- Select a subset of parameters from the pretrained weights to update
- Add a small number of parameters to adapte the (frozen) pretrained model

#### Finetune a subset of parameters

Freezing the first X layers [Lee et al., 2019]



A fourth of the layers need to be fine-tuned to obtain 90% of the performance.

#### Finetune a subset of parameters

**BitFit** [Ben-Zaken et al., 2022]: only finetune the bias term (0.1% of the parameters)

Bias terms in QKV projection

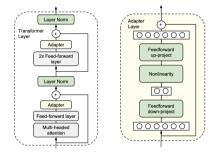
$$egin{aligned} \mathbf{Q}^{m,\ell}(\mathbf{x}) &= \mathbf{W}_q^{m,\ell}\mathbf{x} + \mathbf{b}_q^{m,\ell} \ \mathbf{K}^{m,\ell}(\mathbf{x}) &= \mathbf{W}_k^{m,\ell}\mathbf{x} + \mathbf{b}_k^{m,\ell} \ \mathbf{V}^{m,\ell}(\mathbf{x}) &= \mathbf{W}_v^{m,\ell}\mathbf{x} + \mathbf{b}_v^{m,\ell} \end{aligned}$$

Bias terms in MLP layers

$$\begin{split} \mathbf{h}_{2}^{\ell} &= \mathsf{Dropout}\big(\mathbf{W}_{m_{1}}^{\ell} \cdot \mathbf{h}_{1}^{\ell} + \mathbf{b}_{m_{1}}^{\ell}\big) \\ \mathbf{h}_{3}^{\ell} &= \mathbf{g}_{LN_{1}}^{\ell} \odot \frac{(\mathbf{h}_{2}^{\ell} + \mathbf{x}) - \mu}{\sigma} + \mathbf{b}_{LN_{1}}^{\ell} \\ \mathbf{h}_{4}^{\ell} &= \mathsf{GELU}\big(\mathbf{W}_{m_{2}}^{\ell} \cdot \mathbf{h}_{3}^{\ell} + \mathbf{b}_{m_{2}}^{\ell}\big) \\ \mathbf{h}_{5}^{\ell} &= \mathsf{Dropout}\big(\mathbf{W}_{m_{3}}^{\ell} \cdot \mathbf{h}_{4}^{\ell} + \mathbf{b}_{m_{3}}^{\ell}\big) \\ \mathsf{out}^{\ell} &= \mathbf{g}_{LN_{2}}^{\ell} \odot \frac{(\mathbf{h}_{5}^{\ell} + \mathbf{h}_{3}^{\ell}) - \mu}{\sigma} + \mathbf{b}_{LN_{2}}^{\ell} \end{split}$$

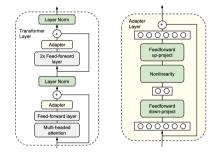
Result: 80.9 (BitFit, 0.08% params) vs 81.8 (full finetuning) on GLUE

#### Adapter [Houlsby et al., 2019]: insert small networks to the pretrained model



- Insert learnable "adapters" in-between layers
- Adapters uses a bottleneck structure to reduce parameters
- Adapters uses a skip-connection

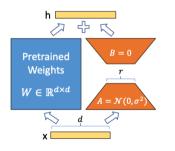
#### Adapter [Houlsby et al., 2019]: insert small networks to the pretrained model



- Insert learnable "adapters" in-between layers
- Adapters uses a bottleneck structure to reduce parameters
- Adapters uses a skip-connection such that it can be "reduced" to the original frozen model

Result: less than 0.4% performance drop with 3% more parameters on GLUE

LoRA [Hu et al., 2021]: add low-rank matrices as additional parameters



Hypothesis: weight matrices are low rank

Adapters: For any matrix multiplication  $h = W_0 x$ , we modify it to

$$h = W_0 x + \Delta W x = W_0 x + BA x$$

• 
$$W_0 \in \mathbb{R}^{d \times k}, B \in \mathbb{R}^{d \times r}, A \in \mathbb{R}^{r \times k} (r \ll k)$$

- Initialization: BA = 0
- Can be applied to any weight matrices, e.g., QKV projection matrices

Compare LoRA and the original adapters:

• LoRA recovers full finetuning by increasing *r* 

Adapter recovers an MLP model with increasing params

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• LoRA recovers full finetuning by increasing *r* 

Adapter recovers an MLP model with increasing params

• LoRA has no additional inference cost by setting  $W_0 \leftarrow W_0 + BA$  (doesn't work for multiple tasks)

Adapter incurs additional inference cost due to the added params

The most widely used efficient finetuning method on very large models (>100B).

Reduce finetuning cost by reducing the number of parameters to update

- Finetune a subset of parameters
- Finetune an additional adapters inserted to the model

Not widely used for SOTA large models, but used sometimes in resource-constrained settings.

Other ways to adapt the model without parameter update: prompting, in-context learning (later)

Lots of open research questions!